

**A. Data Files in MINITAB**

(a)  $\chi^2 = \boxed{135.592}$

(b)  $P\text{-value} = \boxed{0.000}$

(c) Reject  $H_0$  since  $P\text{-value} = 0 < .05 = \alpha$ **B. Chi-Square**

- 9.16

(a)  $df = 2$

(b) Reject  $H_0$  if  $\chi^2 > 5.99$ 

(c)

1.  $H_A$ : Model dress is related to magazine readership  
 $H_0$ : Model dress is not related to magazine readership

2. Using hand calculations,  $\chi^2 = \boxed{80.874}$

3. Reject  $H_0$  since  $\chi^2 = 80.874 > 5.99$

4. There is enough evidence to show that model dress is related to magazine readership.

(d) From MINITAB,  $\chi^2 = 80.874$ ,  $P\text{-value} = 0.000$ (e) Reject  $H_0$  since  $P\text{-value} = 0 < .05 = \alpha$ 

(f)  $p_1$  = proportion of general interest ads which are not sexual  
 $p_2$  = proportion of men's ads which are not sexual

$$\hat{p}_1 = \frac{248}{314} = .7898 \quad \hat{p}_2 = \frac{514}{619} = .8304$$

From MINITAB:  $\boxed{(-0.0944616, 0.0133363)}$ 

Interpret: With 95% confidence,

Between 9.44% fewer and 1.33% more general interest ads than men's ads are not sexual.

(g) The comparison in (f) does not reinforce the  $\chi^2$  test.

The  $\chi^2$  test shows that model dress is related to readership *generally* but the CI doesn't affirm any *specific* difference between general interest ads and men's ads.

(continued)

- (h)  $p_1$  = proportion of women's ads which are sexual  
 $p_2$  = proportion of men's ads which are sexual

$$\hat{p}_1 = \frac{225}{576} = .3906 \quad \hat{p}_2 = \frac{105}{619} = .1696$$

From MINITAB: (0.171382, 0.270612)

Interpret: With 95% confidence,

Between 17.14% and 27.06% more women's ads than men's ads are sexual.

- (i) The comparison in (h) does reinforce the  $\chi^2$  test.

The  $\chi^2$  test shows that model dress is related to readership *generally* and the CI shows where a *specific* difference is.

- (j) Here is the Table of  $\chi^2$  Contributions from MINITAB:

Model Dress	Women	Men	General Interest
Not sexual	12.835	7.227	1.162
Sexual	36.074	20.312	3.265

1. The General Interest/Not Sexual cell contributes the smallest  $\chi^2$  value 1.162.

Also Men/Not Sexual contributes a relatively small 7.227.

So it's not surprising that there are not significant differences between those two categories.

2. The Women/Sexual cell contributes the largest  $\chi^2$  value 36.074.

Also Men/Sexual contributes the second-largest value 20.312.

So it's not surprising to find significant differences between those two categories.

• 9.24

- (a)

Percent of over 40 laid off =  $41/806 = .0508 = 5.08\%$

Percent of under 40 laid off =  $7/511 = .0137 = 1.37\%$

- (b) 1.  $H_A$ : Age is related to being laid off  
 $H_0$ : Age is not related to being laid off

2. Using hand calculations,  $\chi^2 =$  12.303

3. Reject  $H_0$  since  $\chi^2 = 12.303 > 3.84$

4. There is enough evidence to show that age is related to being laid off.

• 9.25

(a)

1.  $H_A$ : Age is related to Performance  
 $H_0$ : Age is not related to Performance
2. Using hand calculations,  $\chi^2 = \boxed{50.812}$
3. Reject  $H_0$  since  $\chi^2 = 50.812 > 5.99$
4. There is enough evidence to show that age is related to performance.

(b) Older employees do appear to perform less well:  $230/758 = 30.3\%$  of them are in the lowest category, compared to  $82/496 = 16.5\%$  of younger employees.

• 9.29

(a)

1.  $H_A$ : City and Income are related  
 $H_0$ : City and Income are not related
2. From MINITAB,  $\chi^2 = \boxed{3.955}$ ,  $P$ -value =  $\boxed{0.412}$
3. Fail to Reject  $H_0$  since  $P$ -value =  $0.412 > .05 = \alpha$
4. There is not enough evidence to show that income is related to city.

(b) There are several pairs of proportions which support the  $\chi^2$  test.  
Here is the pair of categories which have the smallest  $\chi^2$  contributions (0.007 and 0.008):

- (i)  $p_1$  = proportion of City 1 customers with income under \$10,000  
 $p_2$  = proportion of City 2 customers with income under \$10,000

$$\hat{p}_1 = \frac{70}{241} = .2905 \quad \hat{p}_2 = \frac{62}{218} = .2844$$

- (ii) From MINITAB:  $\boxed{(-0.0768405, 0.0889461)}$

Interpret:

We are 95% confident that between 7.68% fewer and 8.89% more City 1 customers than City 2 customers have incomes less than \$10,000.

- (iii) The  $\chi^2$  test does not show any differences in income distributions between City 1 and City 2 customers. The CI confirms this in particular for the lowest income bracket.

### C. Two Means

- 7.58

(b) The two samples are *independent*.

$\mu_1$  = mean satisfaction score for employees with new monitors

$\mu_2$  = mean satisfaction score for employees with standard monitors

From MINITAB, a 95% CI for  $(\mu_1 - \mu_2)$  is

$$(0.060, 2.340)$$

Interpret:

We are 95% confident that employees using new monitors average between 0.06 and 2.34 points higher satisfaction than employees using standard monitors.

(c) Yes, since 0 is not contained in the confidence interval.

- 7.84

1.  $\mu_1$  = mean spatial-reasoning score of children who took piano lessons

$\mu_2$  = mean spatial-reasoning score of children who did not take piano lessons

$$H_A: \mu_1 > \mu_2$$

$$H_0: \mu_1 \leq \mu_2$$

2.  $t = \boxed{5.06}$   $P\text{-value} = \boxed{0.000}$

3. Reject  $H_0$  since

$$P\text{-value} = 0 < .05 = \alpha$$

4. There is conclusive evidence that piano lessons increase children's scores, on average.

- 7.85

95% CI for  $(\mu_2 - \mu_1)$ :  $(-4.508, -1.954)$

Interpret:

We are 95% confident that piano lessons improve children's scores by between 1.95 and 4.51 points, on average.

- 7.10

The two samples are *paired* by household.

1.  $\mu_1$  = mean Vitamin C before cooking, in milligrams/100 grams of blend

$\mu_2$  = mean Vitamin C after cooking, in mg/100 grams of blend

$$H_A: \mu_1 > \mu_2$$

$$H_0: \mu_1 \leq \mu_2$$

2.  $t = \boxed{31.24}$   $P\text{-value} = \boxed{0.000}$

3. Reject  $H_0$  since

$$P\text{-value} = 0 < .05 = \alpha$$

4. There is conclusive evidence that Vitamin C is lost during cooking, on average.

• 7.11

95% CI for  $(\mu_1 - \mu_2)$ : (50.11, 59.89)

Interpret:

We are 95% confident that between 50.11 and 59.89 mg of Vitamin C per 100 grams of blend are lost through cooking, on average.

• 7.43

(a) and (b)

1.  $\mu_1$  = mean Vitamin C in bags at factory, in mg per 100 grams blend  
 $\mu_2$  = mean Vitamin C in bags in Haiti, in mg per 100 grams blend

$$H_A: \mu_1 > \mu_2$$

$$H_0: \mu_1 \leq \mu_2$$

2.  $t = \boxed{4.96}$   $P\text{-value} = \boxed{0.000}$

3. Reject  $H_0$  since

$$P\text{-value} = 0 < .05 = \alpha$$

4. There is conclusive evidence that Vitamin C is lost during shipment from the factory to Haiti, on average.

(c) 95% CI's:

\* Factory: (40.956, 44.748)

\* Haiti: (36.553, 38.484)

\* Difference: (3.12, 7.54)

• 7.47

1.  $\mu_1$  = mean yield of Variety A tomatoes, in pounds  
 $\mu_2$  = mean yield of Variety B tomatoes, in pounds

$$H_A: \mu_1 > \mu_2$$

$$H_0: \mu_1 \leq \mu_2$$

2.  $t = \boxed{1.29}$   $P\text{-value} = \boxed{0.115}$

3. Fail to Reject  $H_0$  since

$$P\text{-value} = 0.115 > .05 = \alpha$$

4. There is not conclusive evidence that Variety A has a higher mean yield than Variety B.

• 7.87

- (a) 1.  $\mu_1$  = mean ego strength of high-fitness professors  
 $\mu_2$  = mean ego strength of low-fitness professors

$$H_A: \mu_1 \neq \mu_2$$

$$H_0: \mu_1 = \mu_2$$

2.  $t = \boxed{8.23}$   $P\text{-value} = \boxed{0.000}$

3. Reject  $H_0$  since

$$P\text{-value} = 0 < .01 = \alpha$$

4. There is overwhelming evidence to show that high-fitness professors and low-fitness professors differ in mean ego strength.

(b) 99% CI: (1.174, 2.405)

- (c) The study shows that ego strength generally depends on the fitness level of college faculty. In fact, the mean ego strength of high-fitness professors exceeds that for low-fitness professors by between 1.17 and 2.41 points.

• 7.46

(a) and (c)

1.  $\mu_1$  = mean pre-test score on Spanish test for executives  
 $\mu_2$  = mean post-test score on Spanish test for executives

$$H_A: \mu_1 < \mu_2$$

$$H_0: \mu_1 \geq \mu_2$$

2.  $t = \boxed{-2.02}$   $P\text{-value} = \boxed{0.029}$

3. • For  $\alpha = .05$ , Reject  $H_0$  since

$$P\text{-value} = 0.029 < .05 = \alpha$$

- For  $\alpha = .01$ , Fail to Reject  $H_0$  since

$$P\text{-value} = 0.029 > .01 = \alpha$$

4. There is sufficient evidence to show that intensive training improves average Spanish scores for executives at a 5% significance level but insufficient evidence at a 1% level.

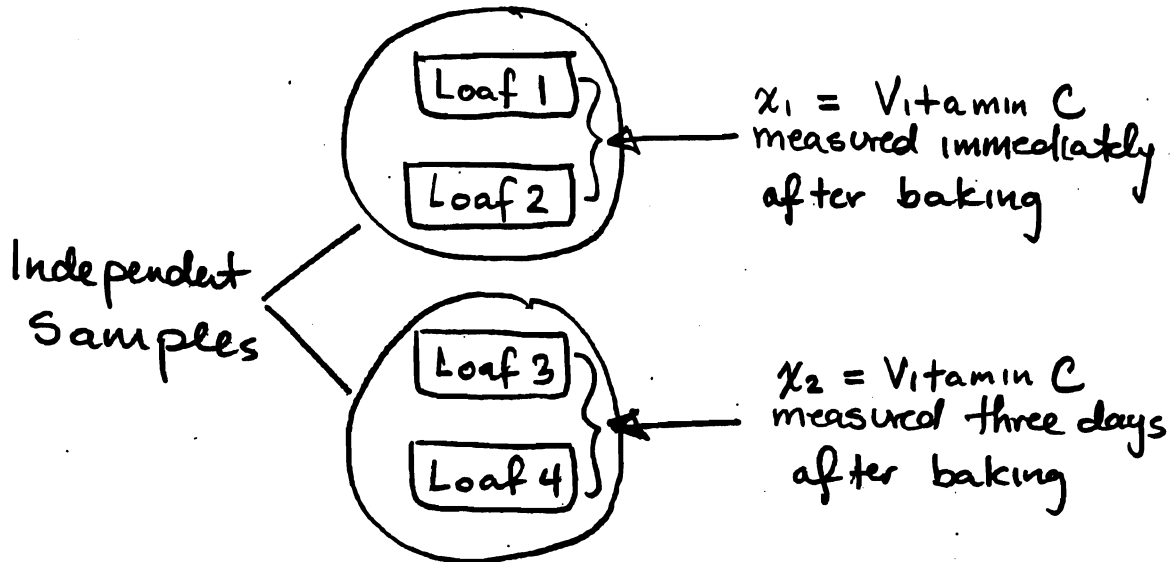
(c) 90% CI: (-2.689, -0.211)

Interpret:

We are 90% confident that intensive training improves Spanish scores for executives by between 0.21 and 2.69 points, on average.

• 7.79

If the loaves of bread are measured as described in this exercise, the samples are *independent* since each measurement is made on a different loaf.



(a)

1.  $\mu_1$  = avg. amount of Vitamin C in loaves of bread immediately after baking, in milligrams/100 grams

$\mu_2$  = avg. amount of Vitamin C in loaves of bread three days after baking, in milligrams/100 grams

$$H_A: \mu_1 > \mu_2$$

$$H_0: \mu_1 \leq \mu_2$$

2.  $t = \boxed{22.16}$   $P\text{-value} = \boxed{0.014}$
3. Reject  $H_0$  since  $P\text{-value} = 0.014 < .05 = \alpha$ .
4. There is sufficient evidence to show that bread loses Vitamin C over three days after baking, on average.

(b) A 90% confidence interval for  $(\mu_1 - \mu_2)$  is

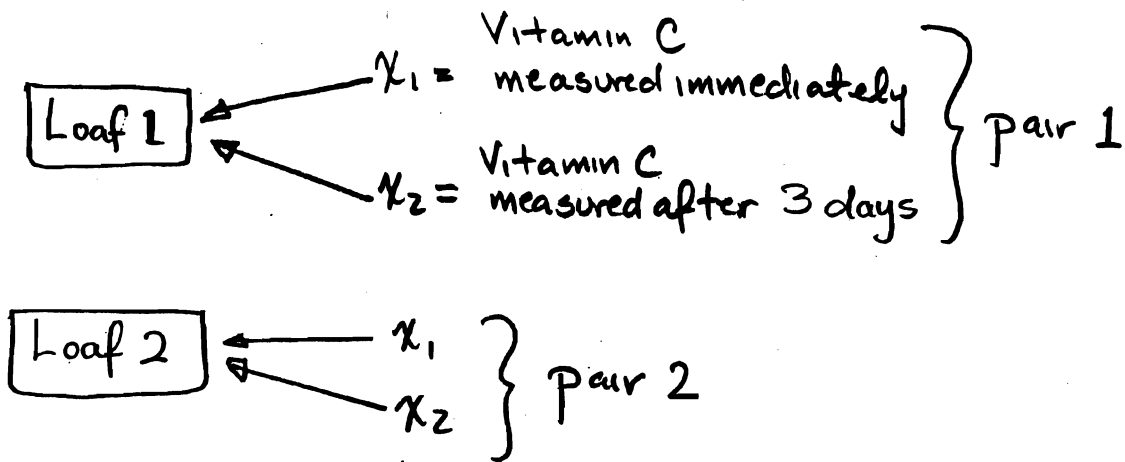
$$(19.24, 34.58)$$

Interpret:

We are 90% confident that loaves of bread lose between 19.24 and 34.58 mg/100g of Vitamin C on average over three days after baking.

• 7.80

If the loaves of bread are measured as described in this exercise, the samples are *paired* by the loaves of bread, each of which is measured twice.



(a)

1.  $\mu_1 = \text{avg. amount of Vitamin C in loaves of bread immediately after baking, in milligrams/100 grams}$

$\mu_2 = \text{avg. amount of Vitamin C in loaves of bread three days after baking, in milligrams/100 grams}$

$$H_A: \mu_1 > \mu_2$$

$$H_0: \mu_1 \leq \mu_2$$

2.  $t = \boxed{49.83}$   $P\text{-value} = \boxed{0.006}$

3. Reject  $H_0$  since  $P\text{-value} = 0.006 < .05 = \alpha$ .

4. There is sufficient evidence to show that bread loses Vitamin C over three days after baking, on average.

(b) A 90% confidence interval for  $(\mu_1 - \mu_2)$  is

$$(23.501, 30.319)$$

Interpret:

We are 90% confident that loaves of bread lose between 23.5 and 30.3 mg/100g of Vitamin C on average over three days after baking.

#### D. Additional

(1)

- (a) The answer is (B)
- (b) Reject  $H_0$  since  $P\text{-value} = 0.034 < 0.05 = \alpha$
- (c) There is enough evidence to show that the average price of diesel exceeds the average price of regular gas at Iowa service stations on Sept. 30, 2012.